

# **An Overview of Intraocular Lens Power Calculation Methods 32**

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Cataract surgery is refractive surgery. Besides removing the dysfunctional cataract, cataract surgery restores and corrects the refractive status of the eye. The success of modern-day cataract surgery is dependent on the refractive outcome. Postoperative refractive surprise is unnecessarily disappointing and frustrating to everyone.

In prescribing the correct glasses, accurate refraction is key to that outcome. In laser cornea refractive surgery, again good preoperative refraction, whether objectively, subjectively, or wavefront-driven, is imperative to a happy result. In cataract surgery, good biometry coupled with good intraocular lens power calculation is crucial to ensure good eventuality. It is akin to accurate refraction in cornea refractive surgery.

In 1949, Harold Ridley implanted a plastic lens in a patient. Despite the less than favorable initial results, he had ushered in a new era of intraocular lenses and indirectly lead to the subsequent development of the science of intraocular lens power calculation.

In the past, IOL power calculation formulas are categorized by generation. However, this can be confusing as formulas evolved and newer methods are being developed. As aptly described by Koch et al., it is opportune to adopt a newer classifcation based on methodology [[1,](#page-9-0) [2](#page-9-1)]. However,

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this has recently been more thoroughly updated by Savini, Hoffer and Kohnen in a recent JCRS Editorial [[2\]](#page-9-1).

# **Historical Methods**

## **Standard Lens Method**

Learning from the poor outcomes of the pioneering implantations, the dioptric power of the early lens implants was adjusted to an improved single-lens power for all patients, depending on what type IOL was used (Prepupillary, Iris Plane or Anterior Chamber). The initial gross refractive errors were reduced. This lasted for almost two decades. This overly simplistic method is obsolete due to the inherently poor outcomes.

## **The Refraction Method**

Among the frst attempts at calculating IOL power was a simple refraction-based method. The power of the IOL was adjusted by a factor of the preoperative refraction.

IOL Power =  $18.00 + 1.25$ <sup>\*</sup> preoperative refraction.

The refraction method has poor outcomes as preoperative refraction with a cataract present is an imprecise method of determining the power

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of the lens. The cataract itself may induce index refractive error that confounds the preoperative refraction.

#### **Theoretical Formulas**

In 1967, Fyodorov and Kolonko [\[3](#page-9-2)] presented their theoretical formula based on geometric optics. The formula utilizesd keratometry and axial length which was measured with A-scan ultrasonography. That marked the nascency of today's geometrical optics or theoretical formulas.

The eye is essentially a 2-lens system. It consists of the cornea as the frst lens that contributes about two-third of the refractive power of the eye; and the crystalline lens that accounts for the remaining one-third of the refracting power of the eye (Fig. [32.1](#page-1-0)). Theoretical formulas using vergence formulas are based on Gaussian optics.

The geometric formulas of Fyodorov and Kolonko [\[3](#page-9-2)] and the other early workers, notably Colenbrander [[4\]](#page-9-3), Thijssen [[5\]](#page-9-4), Van der Heijde [\[6](#page-9-5)], Hoffer [\[7](#page-9-6)] and R Binkhorst (Binkhorst, The optical design of intraocular lens calculation [[8\]](#page-9-7)) are all applied to schematic eyes using theoretical constants. Basically, these formulas use different correction factors but utilize identical vergence concept of:

$$
P = \frac{n}{\text{AL}-\text{ACD}} - \frac{n}{\frac{n}{K} - \text{ACD}}
$$

*Where P is the IOL power; n is aqueous and vitreous refractive index; and ACD the estimated anterior chamber depth that is adjusted by the individual formulaic correction factors.*

The early formulas were good with normal axial lengths of around 23.5 mm (22–24.5 mm) but were less precise with short (<22 mm) or long (>2.5 mm) axial length eyes. Further development on regression and theoretical formulas involved improvement in outcomes in eyes with an expanded range of axial lengths.



The early generation of theoretical formulas assumed fxed postoperative anterior chamber depths. A second generations of theoretical formulas was introduced by Hoffer in 1982, which includes a sub-equation for ELP that mathematically predicts the postoperative effective lens position (ELP) as a function of axial length. The sub-equation (ELP=2.92\*AL-2.93) was based on one IOL model and would be best for that model. R. Binkhorst followed with another iteration. (Binkhorst, Intraocular lens power calculation manual: A guide to the Author's TICC-40 Programs, Edition 3 [[9\]](#page-9-8), [\[10](#page-9-9)] (Hoffer, The effect of axial length on posterior chamber lenses and posterior capsule position [\[11](#page-10-0), [12\]](#page-10-1)). The main difference between these second-generation formulas lies in its prediction of the postoperative effective lens position.

The third generation of theoretical formulas utilizes both AL and keratometry as predictors of preoperative anterior chamber depth (Olsen, Prediction of intraocular lens position after cata-ract extraction [\[13](#page-10-2)]), hence the ELP [[14,](#page-10-3) [15\]](#page-10-4). All these formulas are based on the Gullstrand eye model.

<span id="page-1-0"></span>

## **2-Variables Thin-Lens Vergence Formula: Third Generation Theoretical Formulas**

For the last 3 decades, modern theoretical formulas were the commonly used formulas. These were Hoffer Q, the Holladay, and the SRK/T formulas. These 3 formulas make use of the radius of curvature of the anterior cornea and axial length to predict the ELP. Olsen frst introduced the use of more variable such as the ACD and LT. Later, Holladay introduced his Holladay 2 (Holladay, Holladay IOL Consultant User's Guide and Reference Manual [\[16\]](#page-10-5)) which uses up to 7 variables to predict the ELP. Besides corneal radius and axial length, these include preoperative ACD, phakic lens thickness, the corneal diameter (CD), and the patient's age. Hoffer and Savini later introduced gender and race in their Hoffer H-5 formula.

#### **Hofer Q and Hofer QST**

This formula was published by Kenneth J Hoffer in 1993 (Hoffer KJ, The Hoffer Q formula: a comparison of theoretic and regression formulas [\[17\]](#page-10-6)). The core vergence formula is the basic Hoffer formula (a major modifcation of Colenbrander's formula) but with a new ELP prediction equation he called the Q formula which predicted the ELP based on the AL and the Tangent of the K.

Thanks to the studies by Melles [\[18,](#page-10-7) [19\]](#page-10-8), Hoffer, Savini, and Taroni have further developed a new formula, the Hoffer QST. This is an evolution of the 1993 Hoffer Q formula with the use of AI to enhance the prediction of ELP and algorithms to improve accuracy in the long eyes. There are several studies now showing the Hoffer QST to be as good or better than all the modern formulas depending on the criteria chosen (MAE, MedAE, SD, %+/-0.50 D, etc) [[20](#page-10-9)]. It is freely available on its website www.HofferQST.com with a Research page allowing lens constant (pACD) optimization and IOL power studies on your data.

#### **Holladay 1 and Holladay 2 Formulas**

Holladay's frst formula (Holladay 1) is a 3-part formulation [\[14](#page-10-3)]. The frst part is a set of screening criteria for data. The purpose is to identify the improbable axial length and keratometry measurements and to alert the users to validate the measurements and the possibility of untoward outcomes. He used the Hoffer AJO 1980 study of 7,500 eyes for normal differences in bilateral eyes [\[21](#page-10-10)]. This set of useful checklists has persisted and is now part of most biometry systems but with some modifcations with the changing times. The second part is the formula proper; this is a further modifcation of the second-generation theoretical formula to improve on the prediction of the ELP using Fyodorov's Corneal Height equation (using AL and K). Finally, a personalized "surgeon factor" (SF) (his lens constant) compensates for any systematic bias in the individual surgeon's postoperative outcome.

Holladay's Data Screening Criteria [\[14](#page-10-3)] to identify unusual measurement and require further validation. Repeat measurement if:

- 1. Axial length < 22.0 mm or > 25.0 mm
- 2. Average corneal power < 40.0 Diopters or > 47.0 Diopters
- 3. Calculated emmetropic IOL power > 3.0 Diopters of average power\* for the specifc lens type
- 4. Between eyes, the difference in.
	- (a) Average corneal power > 1.0 Diopter
	- (b) Axial length  $> 0.3$  mm
	- (c) Emmetropic IOL power > 1.0 Diopter

The Holladay 2 formula is unpublished but is available for purchase as part of the Holladay IOL Consultant program (Fig. [32.2\)](#page-3-0). It requires inputs of, besides AL and K, phakic preop ACD, LT, CD and patient's age. Having more parameters enabled the Holladay 2 to appreciate the nuances of disproportionate eyes and render the calculation appropriately.



<span id="page-3-0"></span>

**Fig. 32.2** Holladay JT MD. has categorized human eyes into nine categories (Fig. [32.2](#page-3-0)). This illustrates that the human is not necessarily proportional. This disparity poses a challenge to IOL power calculation, particularly

**SRK/T**

Using the Holladay 1 formula as a base but modifying so it will use the A constant of the SRK formula, Retzlaff published the SRK/T formula [\[15](#page-10-4)] in 1990. The SRK/T is a theoretical formula based on Fyodorov's Corneal Height formula [\[1](#page-9-0)] for the postoperative ELP prediction. The retinal thickness correction factor and the corneal refractive index are likewise optimized.

## **Relationship Between the Third-Generation Formulas and Axial Length**

While most third-generation formulas perform well in normal eyes with axial lengths between 22.0 mm to 25.0 mm, these formulas perform less favorably beyond these confnes. These formulas tend to have a higher percentage of hyperopic prediction errors in longer axial lengths and conversely, myopic outcomes in shorter axial lengths (Fig. [32.3\)](#page-4-0).

#### **Fam Adjusted**

In 2009, Fam et al. [\[22](#page-10-11)] published a paper to optimize the relationship between the predicted refractive outcomes and axial lengths as measured by PCI biometry. The concept was based on 2 readjustments. The frst readjustment, OAL1, was to reverse the initial calibration by Haigis [[23\]](#page-10-12) of the PCI against ultrasound biometry and thereby using the 'actual' optical axial length as measured by the PCI biometer.

in unusual eyes. Fortunately, most of the eyes are normal. Modern IOL power calculation formulas factored in the above into their algorithms

The second adjustment, OAL2, was converting 'actual optical axial length' to 'true optical path length' using the mean refractive index proposed by Olsen [[24\]](#page-10-13). The smaller annulus keratometry measurement with the PCI biometer was also calibrated to the slightly larger mire of autokeratometry. With these adjustments, the performance of the third-generation formulas on longer eyes improved (Fig. [32.4\)](#page-5-0).

#### **Wang-Koch Adjustment**

Wang et al., in 2011 [[25\]](#page-10-14), proposed a set of adjustment equations to optimize the outcomes in eyes longer than 25 mm. The adjustments were shown to reduce the risk of hyperopic outcomes in patients with long eyes. It has been modifed since then.

#### **The T2 Formula**

The T2 formula was described by Sheard, in 2010 [\[26](#page-10-15)]. Using a larger and more up-to-date database, Sheard was able to correct the nonphysiological behavior of the quadratic function of the corneal height prediction of SRK/T frst pointed out by Hoffer and then Haigis [[27\]](#page-10-16).

#### **Haigis Formula**

Haigis realized the importance of lens geometry on the ELP [\[28](#page-10-17)]. Thin lens formulas, by having just a single constant, neglect the effect of changing lens geometry with different IOL power, curvatures, thickness, and styles. In unusual eyes where the almost linear relationship between the ELP and axial length starts to deviate, the perfor-

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**Fig. 32.3** The effect of axial lengths on the prediction errors of 4 theoretical formulas on 4 different IOLs. 3 of the 4 formulas showed hyperopic prediction errors with

long axial lengths. Conversely, the same 3 formulas showed myopic tendency with shorter axial lengths with 3 IOLs

mances of these formulas start to falter. The Haigis formula, without resorting to the complexity of thick lens formulas, uses 3 lens constants  $(a_0, a_1)$  $a_1$   $a_2$ ) instead of one; and using the preopertive measured ACD instead of K as a variable which overcomes some of the problems of thin lens vergence formulas with short and long eyes.

In the Haigis formula, there are 2 types of constant optimization:

- 1. Classical optimization where one constant  $a_0$  is optimized but not the other two. In this case, the formula performs as good, if not better than the other popular thin lens vergence formulas.
- 2. Full optimization where all three constants are optimized. This is when the full potential of the formula for wider ALs and lens types is achieved.

#### **Regression Versus Theoretical Models**

Regression formulas are entirely based on regression with a large database of postoperative outcomes. The larger the database, the better their predictability. More importantly, are the quality

and integrity of the database. In theoretical formulas, regression with real-world postoperative results is utilized to refne its predictability. This is notably so in predicting the effective lens position and is embedded in the constants and correction factors of the formulas. Pure regression formulas (SRK and SRK II) are no longer recommended or used today.

#### **Thin Lens Formula**

The popular 3rd generation formulas for IOL power calculation like the Hoffer Q, Holladay 1, and the SRK/T are based on thin lens optics. A normal lens has a thickness and two refracting surfaces. In thin lens optics, the thickness of the lens is ignored, and its two refracting surfaces are reduced to a single plane thin lens. It is assumed that all refractions of light occur in that single plane. The advantage of the thin lens formula is that it simplifes the calculation and circumvents the diffculty of measuring certain parameters often not obtainable.

The popular formulas of Hoffer Q [\[17](#page-10-6)], Holladay 1  $[14]$  $[14]$ , and SRK/T  $[15]$  $[15]$  are based on thin

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**Fig. 32.4** (**a**) SRK/T outcomes with inputs from PCI. (**b**) SRK/T outcomes with OAL1-K readjustment and (**c**) SRK/T outcomes with OAL2-K readjustment. The abscissas are axial length in mm and the ordinates the prediction error

lens optics. Haigis [\[28](#page-10-17)] subsequently developed an improved thin lens formula by using a thick lens algorithm and regressing the ELP with preoperative data. Unlike the other 3 formulas, Haigis' ELP is derived ELP from the measured axial length and the preoperative anterior chamber depth.

#### **The Impact of Optical Biometry**

In ultrasound biometry, axial length measurement error alone accounted for 54% to 68% of the total prediction error according to Olsen [\[29](#page-10-18)]. With the availability of optical biometry, the source of error from axial length measurement decreased substantially from 0.65 D to 0.43 D or 30 to 40% of the total prediction error according to Olsen [\[30](#page-10-19)]. The repeatability of optical biometry was

reduced from an SD of  $\pm 0.11$  mm to  $\pm 0.03$  mm [\[31](#page-10-20)]. Despite the improvement in AL measurement, this precision is not refected in reducing prediction error according to Olsen [\[30](#page-10-19)]. This less than encouraging improvement was probably overshadowed and supplanted by the ACD prediction error, a function of IOL power calculation formulas [\[31](#page-10-20)].

Newer formulas can leverage the ever improving accuracy of biometric measurement and the quantum leap improvement in computational power to improve the precision and sophistication toward better outcomes and predictability.

In the last decade, many new and better formulas have emerged, making use of the heightened accuracy of the newer biometers and increasing computational power. It is not feasible to go through all the formulas and this article does not claim to be exhaustive.

#### **Ladas Super Formula (LSF) 1.0**

The Hoffer Q, Holladay 1, and SRK/T formulas have different optimal ranges for better outcomes, frst proven and published by Hoffer in 1993. The Ladas Super Formula blends the proven popular formulas of Hoffer Q, Holladay 1 (with and without Wang-Koch adjustment [[25\]](#page-10-14), Haigis and SRK/T using a 3-dimensional model to determine the best power for each eye [\[32](#page-10-21)] based on its 2 to 3 variables inputs. This formula was originally developed by Ladas and subsequently included Siddiqui, Devgan, and Jun. The method has now been enhanced with artifcial intelligence. [www.iolcalc.com.](http://www.iolcalc.com)

#### **Kane Formula**

Developed by Jack X Kane, [[33–](#page-10-22)[35\]](#page-10-23) the Kane formula is an unpublished formula based on theoretical optics with refnements through both regression and artifcial intelligence. It was developed using approximately 30,000 eyes from various cataract practices. The required parameters are AL, K, ACD, and gender with LT and CCT being optional. Various studies have reported excellent outcomes with this formula. The formula is available on [www.iolfomula.com](http://www.iolfomula.com).

#### **Panacea**

This is a thin lens vergence formula developed by David Flikier. It is a 5-variable calculator using AL, K, ACD, LT; and to date the only formula that can utilize the asphericity Q value of the anterior corneal curvature and the anterior-toposterior corneal curvature ratio [\[36](#page-10-24)]. It uses a demographic to statistically data screen the quality of the various inputs. This formula is available only for downloading at [www.panaceaiolan](http://www.panaceaiolandtoriccalculator.com)[dtoriccalculator.com.](http://www.panaceaiolandtoriccalculator.com)

#### **VRF-G**

The VRF is a published vergence-based thin lens formula by Voytsekivskyy [[37\]](#page-10-25). The VRF-G is a newer improved unpublished formula [\[38](#page-10-26), [39\]](#page-10-27). The latter formula is based on theoretical optics with ray-tracing components; further refned through regression. This is an 8-variables formula.

#### **Castrop**

Castrop is a hybrid thin and thick lens formula [\[40](#page-10-28)]. It considers the cornea as a thick lens. It uses a constant like the Olsen C constant and readjusts the axial length based on Cooke's sumof-segments approach. Finally, besides the IOL constant that is integral to the equation, it uses a second constant, offset R to the fnal dioptric power. The formula requires mandatory AL, ACD, and K inputs, with CCT and Post K being optional.

#### **Thick Lens Formula**

The third-generation formulas are simple thin lens formulas that do not require complex calculations. A simple calculator would be sufficient for the formula to be executed. Thin lens formulas are based on the Gullstrand eye model that assumed a fxed ratio of anterior to posterior corneal curvature and a keratometric index of refraction of 1.3375. The systematic deviations of these thin lens assumptions are compensated by the IOL constants. A thin lens formula assumed all the IOL powers of the same IOL model to have the same lens constant. This works reasonably well for the average eye requiring the average IOL power. Despite being the same IOL model, as the IOL power changes: its two curvatures, the ratio of its curvatures, and the lens thickness change. These changes will shift the ELP of the IOL.

Similarly, as the measuring devices become more accurate and comprehensive, more parameters can be measured accurately and be included in the computation of IOL power, without the risk of increasing the errors of propagation.

Barrett Universal II and EVO are thick lens formulas. In simpler terms, these formulas, like the third-generation formulas, predict the ACD of the IOL in the eye. After determining the initial ACD for the eye, the formulas iterate to determine the fnal ELP and thence the fnal IOL power for the eye. These iterative calculations are far more complex and require the power of modern-day computers.

#### **Barrett Universal II (BUII) Formula**

The concept behind the Barrett Universal formula was frst described by Barrett himself in 1987 [\[41](#page-10-29)] and further elucidated in 1993 [\[42](#page-10-30)]. The Barrett Universal II (BUII) is a further refnement of the Barrett Universal formula and includes the use of more variables such as ACD, LT, and radius of curvature of the posterior cornea. These latter additional parameters have reached a high level of precision (with today's optical biometers) to be used confdently.

The BUII heralded in a new era of IOL power calculation formulas, with improved and consistent performances [[43\]](#page-10-31). AL and K inputs are mandatory with ACD, LT, and CD being optional. With the accessibility to corneal thickness (CCT) and posterior corneal curvature (PK) in newer biometers, these variables are now additional optional variables for the formula.

#### **Næser Formula**

Conceptualized by Kristian Næser, this is a paraxial, step-along formula that considers the IOL a thick lens. The difference between Næser 1 [\[44](#page-10-32)] and Næser 2 [\[45](#page-11-0)] are on the source of the IOL architecture. Næser 1 uses the available information on the IOL architecture from the manufacturers (Cutting Card), whereas Næser 2 derived this information from open, commercial but nonproprietary sources. Also, the measured AL is optimized for different axial lengths.

#### **EVO**

Emmetropia Verifying Optical (EVO) formula is a thick lens formula developed by TK Yeo. The formula is based on the emmetropization concept of a normal eye and is constantly updated and improved. Presently, it requires mandatory AL and K inputs, with ACD, LT and CCT being optional, has recently been updated to include posterior cornea curvature.

#### **PEARL-DGS**

This is a thick lens IOL formula that relies on artifcial intelligence of machine learning and modeling to predict ELP and fne-tuning of outputs for extreme biometric values. This formula

was developed by G. Debellemanière, D. Gatinel and A. Saad. The formula is accessible at [iol](https://iolsolver.com)[solver.com](https://iolsolver.com).

#### **Ray Tracing**

Ray tracing is a method for calculating the path of individual rays through the various elements in an optical system. These various elements, with their surfaces and refractive indices, bend and change the passing light path. These individual rays are traced and calculated as they are refracted at each of these surfaces according to Snell's law [[46\]](#page-11-1). Ray tracing may be limited to just the paraxial rays or cover any area on the pupil. The former neglects higher-order aberration, while the latter takes account of them and allows predicting the IOL power that provides the best visual quality.

#### **Olsen Formula**

First published by Olsen in 1987 [\[47](#page-11-2)], this formula has undergone many upgrades and refnement over the years [\[48](#page-11-3), [49\]](#page-11-4). The latest is based on thick-lens ray-tracing optics. The uniqueness of this formula is the C constant concept [\[50](#page-11-5)] that generates the ELP based on the preoperative measurements of ACD and LT but can be additionally tweaked by AL and K, if desirable. The Olsen formula is available as an option in the LenStar biometer or as a standalone PhacoOptics program for purchase ([www.phacooptics.net\)](http://www.phacooptics.net). The Olsen formula (Olsen2P = Olsen 2 parameters) that is preinstalled in biometers uses 2 parameters: ACD and LT to predict the C constant. The Olsen formula (Olsen4P) in the standalone PhacoOptics program uses 4 parameters, besides ACD and LT, AL, and K as well.

#### **Okulix**

Okulix is a standalone computer program that calculates IOL power based on ray-tracing the optical path of single rays that pass through the ocular structure. It uses measured parameters that are fed directly via computer interfacing from the biometers and corneal tomographers. Parameters can also be entered manually, where interfacing is not available. The program includes a compilation of IOL geometry of commonly used IOLs.

#### **CSO Method**

Two corneal tomographers (developed by the Italian company CSO) include a software module that performs IOL power calculations based on exact ray tracing: Sirius is a Scheimpfug-Placido device, and MS 39 is an OCT-Placido instrument. Corneal surfaces as well as actual IOL data are raytraced to calculate the optical performance of the eye and select the IOL power that will produce the targeted refraction or the best visual quality.

#### **Regression Methods**

To improve the accuracy of the early 2nd generation (R Binkhorst, regression formulas were born). The regression formulas are derived empirically from analyzing the relationship between the preoperative biometric measurements and the postoperative refractive outcomes. Using a large outcomes database, the relationship below was established.

## $P \propto A + bK + cAL$

Where *P* is the IOL power, *A* is the *A* constant; *b* and *c* are constants; *K* is the keratometry power and AL is the axial length.

It was frst introduced by Thomas Lloyd (a technician with James Gills) [[51\]](#page-11-6) and followed frst by John Retzlaff [\[52](#page-11-7), [53\]](#page-11-8) and then by Donald Sanders [[54\]](#page-11-9) & Manus Kraff. After the latter 3 combined forces, the SRK formula by Sanders, Retzlaff, and Kraff became the most established regression formula. It underwent subsequent revision (SRK II by Sanders) to compensate for the non-linear relationship between the intraocular lens power and the axial length. The SRK II was popular during the 1980s. It was superseded by the later more accurate 3rd generation theoretical formulas.

#### **Artifcial Intelligence (AI)**

AI examines huge data efficiently and differently from how we humans do; it identifes relationships, patterns, and trends that escape us. AI has been used in medicine, but these are mainly for image classifcation and object recognition. IOL power calculation is now benefting from AI as well.

Critical to the success of AI is a large and sound "training" dataset. AI learns from its dataset through interpreting and unraveling, to achieve the desired goal. An accurate and consistent dataset is indispensable to good machine learning. With a large and accurate dataset, AI can fgure out the complex relationships between the many biometric parameters that may not ft traditional eye models or Gaussian optics.

Datasets from different devices may have to be interpreted differently, or at the very least adjusted and optimized to the device. Newer IOLs with novel optical structures that have yet to attain a sufficient sizable dataset may pose a challenge for AI. As AI learning capabilities improve, it may be able to adapt to parameters from different devices and bridge newer IOLs.

Despite these challenges, the future of AI is bright. It has already markedly improved outcomes as shown by some formulas such as RBF 3.0, Hoffer QST and PEARL-DGS. As the datasets get larger, these formulas improve further as typifed by the version numbers. More and more parameters are being utilized as the neuronal circuits are refned and expanded.

#### **Radial Basis Function (RBF)**

Developed by Hill and his team, this formula is based on radial basis function (RBF), a machinelearning form of artifcial intelligence. RBF with its multidimensions pattern recognition and adaptive neural learning process is appropriate to these real-world challenges of IOL power calculation. The formula is constantly being updated as more and more data is available to refne

the process. At last look, the formula has been updated to version 3.0 with an expanded domain.

RBF is available as an option on some devices as well as online at [www.rbfcalculator.com.](http://www.rbfcalculator.com) The required variables are AL, K, and ACD with LT, CCT, and CD as options.

### **BART**

This update on the development of Bayesian Additive Regression Trees (BART) [\[55](#page-11-10)] was described by Clarke et al. in 2020. This is an AI method using a machine-learned algorithm that sums decision trees. It gauges its accuracy using Monte Carlo simulations and generates intervals of possible lens powers with a probability density. Over a fvefold cross-validation process, the result of BART was an SD of 0.242 D compared to 0.416 (Holladay 1), 0.569 D (RBF 1.0), 0.575 D (SRK/T), 0.936 D (Hoffer Q), and 1.48 D (Haigis). The results were without optimizing the constants (which might be unfair to some of the formulas). MedAE was 0.204 D (BART), 0.416 D (Holladay 1), 0.676 D (RBF 1.0), 0.714 D (SRK/T), 0.936 D for Hoffer Q, and 1.204 D for Haigis. BART prediction achieved 89.5% within +/-0.50 D of prediction error, RBF 1.0 was 61.4%, and SRK/T with 52.0%.

#### **Ladas Super Formula (LSF) 2.0**

This formula uses machine learning algorithms to refne the prediction of the original LSF 1.0. using AL, K, and ACD as inputs. In a sample of 101 eyes implanted with the same IOL Taroni found in 2020, that this formula was one of the best performers among several modern formulas with a median absolute error of 0.22 D [[56\]](#page-11-11).

#### **Intraoperative Aberrometry**

#### **ORA**

Optiwave Refractive Analysis (ORA) is a methodology frst proposed by Ianchulev in 2005 [\[57](#page-11-12), [58](#page-11-13)]. This intraoperative Talbot-Moiré interferometry measures the ocular wavefront aberrations after removal of the crystalline lens in surgery. The captured real-time wavefront information is used to determine the aphakic spherical equivalent of the eye and thence calculate the proper desired IOL power. The system is independent of AL and K.

#### **Conclusion**

Today, there is an explosion of new IOL power calculation formulas and methods. This is a welcome development, as today patients are expecting better refractive outcomes. The newer formulas have shown to be more accurate than the once eminently popular third-generation formulas. As the hardware and computational power improve, we can expect even better formulas [[1\]](#page-9-0).

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